

RECSM Summer School: Machine Learning for Social Sciences

Session 2.4: Boosting

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Boosting

Boosting

- Like bagging, boosting is a **general approach** that can be applied to many machine learning methods for regression or classification.
- Recall that **bagging** creates multiple bootstrap training sets from the original training set, fits a separate tree to each bootstrap training set, and then combines all trees to create a single prediction.
- This means that each tree is built on a bootstrap sample, **independent** of the other trees.

Boosting

- In boosting, the trees are grown **sequentially**: each tree is grown using information from previously grown trees.
- Boosting does not involve bootstrap sampling. Instead, each tree is fit on a **modified version** of the original data set.

Boosting

Algorithm

Algorithm: Boosting for Regression Trees

- 1 Set $\hat{f}(x) = 0$ and $r_i = y_i$ for all i in the training set.
- 2 For $b = 1, 2, \dots, B$, repeat:
 - (a) Fit a tree \hat{f}^b with d splits ($d + 1$ terminal nodes) to the training data (X, r) .
 - (b) Update \hat{f} by adding in a shrunk version of the new tree

$$\hat{f}(x) \leftarrow \hat{f}(x) + \lambda \hat{f}^b(x). \quad (2.4.1)$$

- (c) Update the residuals

$$r_i \leftarrow r_i - \lambda \hat{f}^b(x_i). \quad (2.4.2)$$

- 3 Output the boosted model

$$\hat{f}(x) = \sum_{b=1}^B \lambda \hat{f}^b(x). \quad (2.4.3)$$

Boosting

What Is the Idea Behind Boosting?

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- Unlike fitting a single large decision tree, which potentially overfits the data, boosting **learns slowly**.
- Given the current model, we fit a new decision tree to the **residuals** from that model (rather than the outcome Y).
- We then add the new decision tree into the fitted function in order to **update the residuals**.

What Is the Idea Behind Boosting?

- Each of the trees can be rather **small**, with just a few terminal nodes, determined by parameter d .
- Fitting **small** trees to the residuals means that we **slowly improve** \hat{f} in areas where it does not perform well.
- The shrinkage parameter λ **slows the process even further**, allowing **more** and **different shaped** trees to attack the residuals.

Boosting

Tuning Parameters for Boosting

Tuning Parameters for Boosting

① Number of trees B

- Boosting can **overfit** if B is too large.
- Use **CV** to select B .

② Shrinkage parameter λ

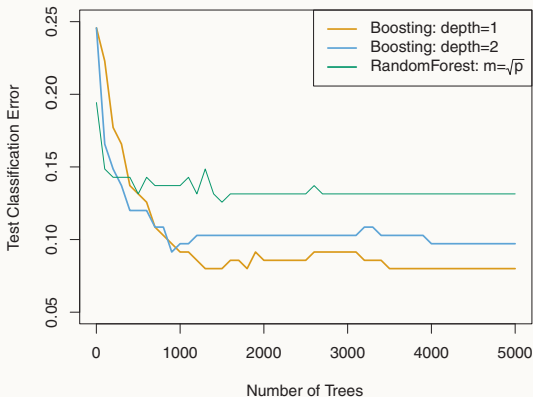
- Controls the **rate** at which boosting learns.
- A small positive number, typical values are 0.01 or 0.001.
- Very small λ can require a **very large value of B** in order to achieve good performance.

Tuning Parameters for Boosting

- ③ Number of splits in each tree d
 - Controls the **complexity** of the boosted ensemble.
 - It is the **interaction depth**, since d splits can involve at most d variables.
 - Often $d = 1$ works well, in which case each tree is a **stump** (consisting of a single split).

Boosting – Gene Expression Example

Boosting and Random Forests Applied to Gene Expression Data



(Boosting with stumps, if enough of them are included, outperforms the depth-two model. Both boosting models outperform a random forest. Source: James et al. 2013, 324)

For the two boosted models, $\lambda = 0.01$. Note that the test error rate for a single tree is 24%.